



education

Department:
Education
North West Provincial Government
REPUBLIC OF SOUTH AFRICA

PROVINCIAL ASSESSMENT *PROVINSIALE ASSESSERING*

GRADE 11/GRAAD 11

MATHEMATICS P1/WISKUNDE VI

JUNE/JUNIE 2024

MARKING GUIDELINES/NASIENRIGLYNE

MARKS/PUNTE: 100

These marking guidelines consist of 8 pages.
Hierdie nasienriglyne bestaan uit 8 bladsye.

NOTE:

- If a candidate answered a question TWICE, only mark the FIRST attempt.
- Consistent accuracy applies in ALL aspects of the marking memorandum.

NOTA:

- Indien 'n kandidaat 'n vraag TWEE KEER beantwoord het, word slegs die EERSTE poging nagesien.
- Volgehoue akkuraatheid word DEURGAANS in die memorandum toegepas.

QUESTION/ VRAAG 1

1.1	$x(x - 3) = 40$	
1.1.1	$x^2 - 3x - 40 = 0$ $\therefore (x - 8)(x + 5) = 0$ $\therefore x = 8 \text{ or } x = -5$	✓ std form/stdvorm ✓ factors/faktore ✓ both answers/beide antwe (3)
1.1.2	$3x^2 - 2x - 4 = 0$ $\therefore x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(3)(-4)}}{2(3)}$ $\therefore x = 1,54 \text{ or } x = -0,87$	✓ subst ✓✓ each answ/elke antw (3)
1.1.3	$\sqrt{x - 3} + 1 = \frac{12}{\sqrt{x-3}}$ Let / Laat $\sqrt{x - 3} = k$ $\therefore k + 1 = \frac{12}{k}$ $\times k: k^2 + k = 12$ $\therefore k^2 + k - 12 = 0$ $\therefore (k + 4)(k - 3) = 0$ $\therefore k = -4 \text{ or } k = 3$ $\therefore \sqrt{x - 3} = -4 \text{ or } \sqrt{x - 3} = 3$ no solution/geen opl or / of $x - 3 = 9$ $x = 12$	✓ × LCM/KGV ✓ factors/faktore ✓ - 4 & 3 ✓ no sol/ geen opl ✓ square /kwadreer ✓ $x = 12$

OR / OF:

	$\sqrt{x-3} + 1 = \frac{12}{\sqrt{x-3}}$ $\times \sqrt{x-3}: (\sqrt{x-3})^2 + \sqrt{x-3} = 12$ $\therefore x - 3 + \sqrt{x-3} = 12$ $\therefore \sqrt{x-3} = 15 - x$ $\therefore x - 3 = 225 - 30x + x^2$ $\therefore x^2 - 31x + 228 = 0$ $\therefore (x-19)(x-12) = 0$ $\therefore x = 19 \text{ or } \text{ of } x = 12$ <p>but/maar $x \neq 19$ (def $\sqrt{\square}$) \therefore slegs $x = 12$ only</p>	✓ $\times LCM/KGV$ ✓ isol $\sqrt{\square}$ ✓ square/kwadr ✓ factors/faktore ✓ $x \neq 19$ ✓ $x = 12$ (6)
1.1.4	$2 - 16x^{-\frac{3}{2}} = 0$ $\therefore x^{-\frac{3}{2}} = \frac{1}{8}$ $\therefore x = (2^{-3})^{-\frac{2}{3}}$ $\therefore x = 2^2 = 4$	✓ $\frac{1}{8}$ ✓ 2^{-3} ✓ $\exp -\frac{2}{3}$ ✓ $x = 4$ (4)
1.1.5	$9^{2x} + 9 = 10 \cdot 3^{2x}$ $\therefore (3^2)^{2x} + 9 = 10 \cdot 3^{2x}$ <p>Let / Laat $3^{2x} = k$:</p> $\therefore k^2 + 9 = 10k$ $\therefore k^2 - 10k + 9 = 0$ $\therefore (k-9)(k-1) = 0$ $\therefore k = 9 \text{ or } \text{ of } k = 1$ $\therefore 3^{2x} = 9 = 3^2 \text{ or } \text{ of } 3^{2x} = 1 = 3^0$ $\therefore 2x = 2 \text{ or } \text{ of } 2x = 0$ $\therefore x = 1 \text{ or } \text{ of } x = 0$	✓ $9 = 3^2$ ✓ std form ✓ factors/faktore ✓ both eq/beide vgl ✓ $x = 1$ ✓ $x = 0$ (6)

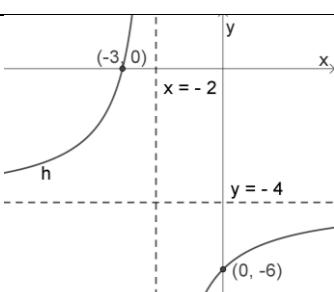
1.2	$x - 3y = 1 \dots \quad \textcircled{1}$ $x^2 - 2xy + 9y^2 = 17 \dots \textcircled{2}$ from / uit $\textcircled{1}$: $x = 3y + 1$ subst in $\textcircled{2}$: $(3y + 1)^2 - 2y(3y + 1) + 9y^2 = 17$ $\therefore 9y^2 + 6y + 1 - 6y^2 - 2y + 9y^2 - 17 = 0$ $\therefore 12y^2 + 4y - 16 = 0$ $\therefore 3y^2 + y - 4 = 0$ $\therefore (3y + 4)(y - 1) = 0$ $\therefore y = -\frac{4}{3} \text{ or } \text{ of } y = 1$ if / as $y = -\frac{4}{3}$: $x = 3\left(-\frac{4}{3}\right) + 1 = -3$ if / as $y = 1$: $x = 3(1) + 1 = 4$	✓ x subject/onderwerp ✓ subst ✓ std form ✓ faktore/factors ✓ both y-values/beide y-w ✓ both x-values/beide x-w (6)
1.3	$-b = 3 \therefore b = -3$	✓ $b = -3$
1.3.1	$-4ac = 16a \therefore c = -4$	✓ $c = -4$ (2)
1.3.2	$a = 1$, $9 + 16(1) = 25 \therefore \text{complete square/volkome vierk}$	✓ $a = 1$ ✓ comp sq/ volk vierk (2)
1.4.1	$x^2 - 2x - 3 < 0$ $\therefore (x - 3)(x + 1) < 0$  $\therefore -1 < x < 3$	✓ < 0 ✓ factors/faktore ✓ method & critical values <i>Metode & kritiese waardes</i> ✓ answ/ antw (4)
1.4.2	$x = -5$	✓ answ/antw (1)
1.5	$n^{500} < 6^{200}$ $\therefore (n^5)^{100} < (6^2)^{100}$ $\therefore n^5 < 6^2$ $\therefore n^5 < 36$ $\therefore n = 2 \quad (2^5 = 32)$	✓ $(\square)^{100} \text{ or } \text{ of } \sqrt[100]{\square}$ ✓ < 36 ✓ $n = 2$ (3) [40]

QUESTION 2

2.1 2.1.1	$\begin{aligned}\frac{\sqrt{3}}{\sqrt{3}+1} &= \frac{\sqrt{3}}{\sqrt{3}+1} \times \frac{\sqrt{3}-1}{\sqrt{3}-1} \\ &= \frac{3-\sqrt{3}}{3-1} \\ &= \frac{3-\sqrt{3}}{2}\end{aligned}$	✓ $\times \frac{\sqrt{3}-1}{\sqrt{3}-1}$ ✓ $3 - \sqrt{3}$ (numerator/teller) ✓ 2 (denominator/noemer) (3)
2.1.2	$\begin{aligned}\frac{5^{3n+5}}{125^{n+1}} &= \frac{5^{3n+5}}{(5^3)^{n+1}} \\ &= \frac{5^{3n+5}}{5^{3n+3}} \\ &= 5^2 = 25\end{aligned}$	✓ $125 = 5^3$ ✓ exp law / eksp wet $3n+3$ ✓ 25 (3)
2.1.3	$\begin{aligned}-5\sqrt{48a^8} + 3\sqrt{27a^8} &= -5\sqrt{3 \cdot 16a^8} + 3\sqrt{3 \cdot 9a^8} \\ &= -5(4a^4)\sqrt{3} + 3(3a^4)\sqrt{3} \\ &= -20a^4\sqrt{3} + 9a^4\sqrt{3} \\ &= -11a^4\sqrt{3}\end{aligned}$	✓ $48 = 16 \cdot 3$ & $27 = 9 \cdot 3$ ✓ $-20a^4\sqrt{3}$ ✓ $9a^4\sqrt{3}$ ✓ $-11a^4\sqrt{3}$ (4)
2.1.4	$\begin{aligned}\frac{4 \cdot 5^x - 2 \cdot 5^{x+1}}{5^{x-1} - 5^x} &= \frac{5^x(4 - 2 \cdot 5^1)}{5^x(5^{-1} - 1)} \\ &= \frac{(4 - 10)}{\left(\frac{1}{5} - 1\right)} \\ &= \frac{-6}{\frac{-4}{5}} = -6 \times -\frac{5}{4} = \frac{15}{2}\end{aligned}$	✓ $5^x(4 - 2 \cdot 5^1)$ ✓ $5^x(5^{-1} - 1)$ ✓ $\frac{1}{5}$ ✓ $\frac{15}{2}$ (4)
2.1.5	$\begin{aligned}\sqrt{\frac{2^{2020} + 2^{2025}}{33(2^{2014})}} &= \sqrt{\frac{2^{2020}(1+2^5)}{33(2^{2014})}} \\ &= \sqrt{\frac{2^{2020}(33)}{33(2^{2014})}} \\ &= \sqrt{2^6} = 2^3 = 8\end{aligned}$	✓ CF/GF ✓ 33 cancel/kanselleer ✓ $\sqrt{2^6}$ ✓ 8 (4)

2.2	<p>Let / Let $1234567892 = k$</p> $\therefore 1234567893 \times 1234567894 - 1234567895 \times 1234567892$ $= (k+1)(k+2) - (k+3)(k)$ $= k^2 + 3k + 2 - k^2 - 3k$ $= 2$ <p>OR / OF</p> <p>Let / Let $1234567893 = n$</p> $\therefore 1234567893 \times 1234567894 - 1234567895 \times 1234567892$ $= n(n+1) - (n+2)(n-1)$ $= n^2 + n - (n^2 + n - 2)$ $= 2$ <p>OR similar subst / OF soortgelyke subst</p>	✓ method/metode ✓ subst ✓ 2 (3) [21]
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QUESTION 3

3.1	$x = -2$ $y = -4$	✓ ✓ each equation / elke vgl (2)
3.2	$h(0) = \frac{-4}{0+2} - 4 = -6 \quad \therefore (0; -6)$ $0 = \frac{-4}{x+2} - 4$ $\therefore 4 = \frac{-4}{x+2}$ $\therefore 4(x+2) = -4$ $\therefore 4x + 8 = -4$ $\therefore 4x = -12$ $\therefore x = -3 \quad \therefore (-3; 0)$	✓ $y = -6$ ✓ $y = 0$ ✓ $x = -3$ (3)
3.3		✓ asymptotes/asimptote ✓ $(-3; 0)$ ✓ $(0; -6)$ ✓ shape/vorm (4)
3.4	$\frac{-4}{x+2} - 4 \geq 0 \quad \therefore -3 \leq x < -2$	✓ interval ✓ notation/notasie (2) [11]

QUESTION 4

4.1	$y > -6 ; y \in \mathbb{R}$	✓ (1)
4.2	$f(x) = a \cdot b^x - 6 \quad \text{Subst } (0; -3):$ $\therefore -3 = ab^0 - 6$ $\therefore 3 = a$ $\therefore f(x) = 3b^x - 6 \quad \text{subst } (-1; 0)$ $\therefore 0 = 3b^{-1} - 6$ $\therefore \frac{6}{3} = \frac{1}{b}$ $\therefore 2b = 1$ $\therefore b = \frac{1}{2}$	✓ $q = -6$ ✓ subst $(0; -3)$ ✓ $a = 3$ ✓ subst $(-1; 0)$ ✓ $b = \frac{1}{2}$ (5)
4.3	$18 = 3 \left(\frac{1}{2}\right)^x - 6$ $\therefore 24 = 3 \left(\frac{1}{2}\right)^x$ $\therefore 8 = 2^{-x}$ $\therefore 2^3 = 2^{-x}$ $\therefore x = -3$	✓ subst 18 ✓ 8 ✓ exp form/eksp vorm ✓ $x = -3$ (4)
4.4	$-y = 3 \left(\frac{1}{2}\right)^x - 6$ $\therefore g(x) = -3 \left(\frac{1}{2}\right)^x + 6 \quad \text{OR/OF}$ $g(x) = -3(2)^{-x} + 6$	✓ $-3 \left(\frac{1}{2}\right)^x$ of $-3(2)^{-x}$ ✓ +6 [12]

QUESTION 5

5.1	For A & B: $g(x) = x^2 - 6x - 16 = 0$ $\therefore (x - 8)(x + 2) = 0$ $\therefore x = 8 \text{ or } \text{ of } x = -2$ $\therefore A(-2; 0) \text{ & } B(8; 0) \therefore AB = 10 \text{ units} \text{ eenhede}$	✓ $g(x) = 0$ ✓ factors/faktore ✓ 10 (3)
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5.2	$x = \frac{-b}{2a} = \frac{-(-6)}{2(1)} = 3 \quad \text{or} \quad x = \frac{8+(-2)}{2} = 3$ $\begin{aligned} g(3) &= (3)^2 - 6(3) - 16 \\ &= -25 \end{aligned} \quad \therefore D(3; -25)$ <p>OR/OF</p> $\begin{aligned} g(x) &= x^2 - 6x + 9 - 9 - 16 \\ &\therefore g(x) = (x - 3)^2 - 25 \\ &\therefore D(3; -25) \end{aligned}$	✓ $x = 3$ ✓ subst 3 / $g(3)$ ✓ $y = -25$ (3) ✓ compl square/kwadr voltooï ✓ $x = 3$ ✓ $y = -25$ (3)
5.3	For Q : $g(x) = f(x)$ $\therefore x^2 - 6x - 16 = -x - 2$ $\therefore x^2 - 5x - 14 = 0$ $\therefore (x - 7)(x + 2) = 0$ $\therefore x = 7 \text{ or } \text{ of } -2$ for Q: $f(7) = -7 - 2 = -9 \therefore Q(7; -9)$	✓ equating / gelykstel ✓ factors ✓ choose / kies/subst $x = 7$ ✓ $y = -9$ (4)
5.4		
5.4.1	$-2 < x < 7$	✓ interval ✓ notation (2)
5.4.2	$x \geq 8 \quad \text{or} \quad \text{ of } \quad x = -2$	✓ $x \geq 8$ ✓ $x = -2$ (2)
5.4.3	$0 < k < 9$	✓ interval ✓ notation (2) [16]
		TOTAL/TOTAAL: 100

MATHEMATICS P1 GR 11

Jun-24

TAXONOMY

Question / Level	1	2	3	4	TOT	ONDERWERP	Real	Expected	
							subtotal	per topic	
1.1.1	3				3	vgl			EQUATIONS & INEQUALITIES
1.1.2	3				3	vgl			
1.1.3			6		6	vgl met wortel, breuk			
1.1.4		4			4	eksp vgl			
1.1.5			6		6	eksp vgl			
1.2		6			6	gelykt vgl			
1.3.1			2		2	formula			
1.3.2			2		2	aard v wortels			
1.4.1			4		4	aard v wortels			
1.4.2	1				1	aard v wortels			
1.5				3	3	eksp inequality	40	40	
2.1.1		3			3	eksp			
2.1.2		3			3	eksp			
2.1.3		4			4	eksp			
2.1.4		4			4	eksp			
2.1.5				4	4	eksp			
2.2				3	3	algebra	21	20	ALGEBRA
3.1	2				2	hyperbola			
3.2	3				3	hyperbola			
3.3		4			4	hyperbola			
3.4			2		2	hyperbola	11		
4.1	1				1	eksp f			EXP FUNC
4.2		5			5	eksp f			
4.3		4			4	eksp f			
4.4		2			2	eksp f	12		
5.1		3			3	parab & lyn			
5.2	3				3	parab & lyn			PARABOLA & LINE
5.3			4		4	parab & lyn			
5.4.1			2		2	parab & lyn			
5.4.2				2	2	parab & lyn			
5.4.3				2	2	parab & lyn	16		
ACTUAL TOT:	16	42	28	14	100		100		
ACTUAL % :	16	42	28	14	100				
EXPECT.%	20%	35%	30%	15%	100%				